

## Orbital Phase Continuity Requirements in Triplet States

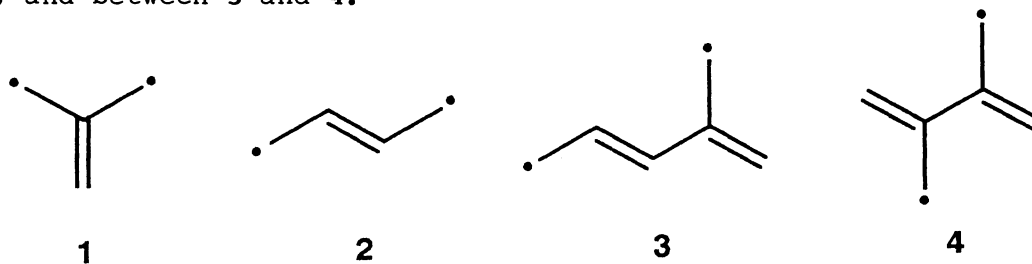
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Orbital phase continuity requirements were derived for stabilizing triplet states, and successfully applied to acyclic conjugated diradicals.

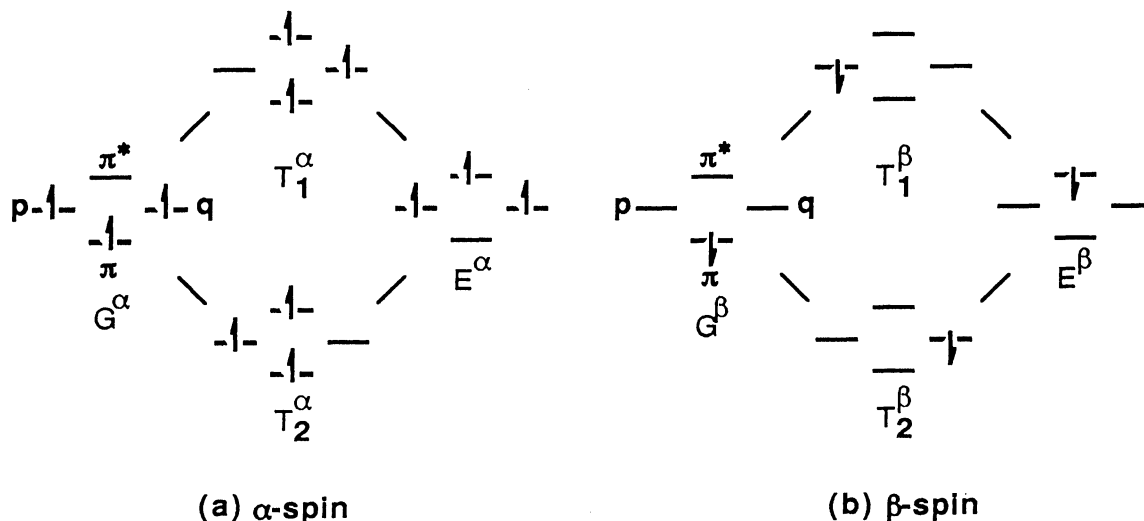
Triplet states of molecules are important intermediates in photochemical processes.<sup>1)</sup> Triplet diradicals receive an increasing interest as prototypes of high-spin molecules for molecular based magnetic materials.<sup>2)</sup> In this letter we will present an orbital phase theory for the stabilities of triplet states and apply it to some conjugated diradicals 1-4.

In 1-4, two radical centers do not effectively interact with each other, but with an intervening conjugated coupler. The coupler is an ethylene unit in 1 and 2, and a butadiene unit in 3 and 4. The modes of connection of the radical centers and the couplers are different between 1 and 2, and between 3 and 4.



The mechanism of electron delocalization and polarization is illustrated in Scheme 1. An  $\alpha$ -spin electron occupies each of the radical orbitals,  $p$  and  $q$ , and the HOMO ( $\pi$ ) of the coupler in the ground configuration ( $G^\alpha$ ). The electron in one of the radical centers ( $p$ ) shifts to the LUMO ( $\pi^*$ ) of the coupler through the interaction of  $G^\alpha$  and the transferred configuration ( $T_1^\alpha$ ). The  $G^\alpha$ - $T_1^\alpha$  interaction is approximated to the  $p$ - $\pi^*$  interaction. The resulting electron hole in the radical center  $p$  is supplied with an electron from  $\pi$  of the coupler through the interaction

of  $T_1^\alpha$  and the locally-excited configuration ( $E^\alpha$ ), or the  $\pi$ -p interaction. The  $\pi$ -p- $\pi^*$  interaction is involved in the delocalization-polarization process. There is another process involving the  $G^\alpha$ - $T_2^\alpha$ - $E^\alpha$  or  $\pi$ -q- $\pi^*$  interaction. As a result, cyclic  $[G^\alpha-T_1^\alpha-E^\alpha-T_2^\alpha]$  or  $[\pi$ -p- $\pi^*$ -q] interaction occurs.



Scheme 1.

For effective occurrence of the cyclic interaction, simultaneous bonding properties are required between any pair of configurations:

$$S(G^\alpha, T_1^\alpha)S(T_1^\alpha, E^\alpha)S(E^\alpha, T_2^\alpha)S(T_2^\alpha, G^\alpha) > 0 \quad (1)$$

where  $S$  is an overlap integral between configurations. The inequality is rewritten as

$$s(p, \pi^*)s(\pi, p)s(q, \pi^*)s(\pi, q) > 0 \quad (2)$$

where  $s$  denotes orbital overlap integral.

Delocalization-polarization mechanism of  $\beta$ -electrons is shown in Scheme 1b. An electron shifts from  $\pi$  to  $p$  through the  $G^\beta$ - $T_1^\beta$  or  $\pi$ -p interaction. The electron then shifts to  $\pi^*$  through the  $T_1^\beta$ - $E^\beta$  or  $p$ - $\pi^*$  interaction. The  $G^\beta$ - $T_1^\beta$ - $E^\beta$  or  $\pi$ -p- $\pi^*$  interaction is involved. The other process involves the  $G^\beta$ - $T_2^\beta$ - $E^\beta$  interaction or the  $\pi$ -q- $\pi^*$  interaction. The cyclic  $[G^\beta-T_1^\beta-E^\beta-T_2^\beta]$  or  $[\pi$ -p- $\pi^*$ -q] interaction similarly occurs in the  $\beta$ -spin delocalization-polarization process. The same inequality (2) was obtained.

The inequality requirements can be easily seen to be equivalent to simultaneous satisfaction of the orbital phase continuity conditions: 1) the electron donating orbitals out of phase; 2) the accepting orbitals in phase; 3) the donating and accepting orbitals in phase. The p and q orbitals at the radical centers are the donating orbitals for  $\alpha$ -spin and the accepting orbitals for  $\beta$ -spin. The phase conditions are essentially the same as those for cyclic<sup>3)</sup> and acyclic<sup>4)</sup> closed-shell molecules.

The diradicals 1 and 3 meet the phase requirements in both spin spaces. The orbital phase is continuous. This is not the case with their isomers, 2 and 4. The phase is discontinuous. Consequently, triplet states of 1 and 3 are thermodynamically stable relative to 2 and 4, respectively. This agrees with known relative stabilities found in literatures.<sup>5)</sup>

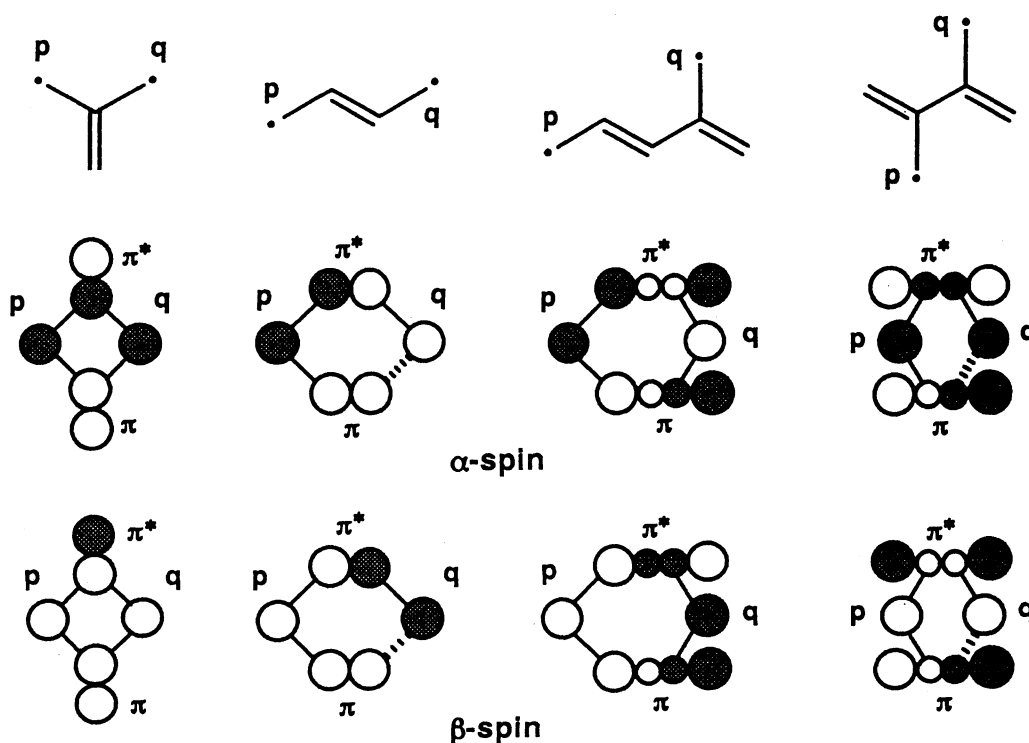


Table 1. Coefficient Ratios of Locally-Excited and Electron-Transferred Configurations to the Ground Configuration

Triplet diradical	$E^\alpha$	$T_1^\alpha$	$T_2^\alpha$	$E^\beta$	$T_1^\beta$	$T_2^\beta$
1	0.49	0.25	0.25	0.50	0.25	0.25
2	0.0	0.15	0.15	0.0	0.13	0.13
3	0.62	0.30	0.17	0.60	0.30	0.17
4	0.0	0.26	0.26	0.0	0.27	0.27

We carried out ab initio UHF calculations<sup>6)</sup> on the triplet states of these diradicals. The total wave functions were subjected to the open-shell configuration analysis. The results (Table 1) supported the orbital phase predictions. Contributions of the local-excitation of both spins are significant in 1 (0.49 for  $E^\alpha$  and 0.50 for  $E^\beta$ ), whereas absent in 2. Electron delocalization or mixing of the transferred configurations also prefers 1 (0.25 for both spins) to 2 (0.15 for  $\alpha$  and 0.13 for  $\beta$ -spin). This is understood as the results of the orbital phase continuity (1) and discontinuity (2). The effect of the orbital phase is outstanding in the polarization rather than the delocalization. There are great contributions from the polarization in 3, but not at all in 4. This is also understood due to the continuity (3) and discontinuity (4) of orbital phase.

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